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In [ ]: # HIDDEN
from datascience import *
%matplotlib inline
import matplotlib.pyplot as plots
plots.style.use('fivethirtyeight')
import numpy as np
```

Data 8 Fall 2016 Midterm Review 10/12/16
Discussion of exam conditions; see video

Intervals and Bins

at least 7: ≥ 7
at most 7: ≤ 7
more than 7: > 7
between 2 and 7 inclusive: includes both end points

Python convention: intervals include the left end point
but not the right
are.between: includes left, excludes right
tbl.hist: bins include left, exclude right
np.arange(start, end, step): includes start, excludes end

Histograms

- Quantitative data
- Horizontal axis drawn to scale
- Area of bar proportional to number/proportion/percent of entries in bin
- Height = area/width
- Density scale: Height = proportion/width, total area = 1
- Equivalent to percent/width, total area = 100
- Height measures crowdedness
- Statements like: "The left half of the bar contains half the proportion in the bar" assume that the entries are evenly distributed within the bar

Variable: length, measured in inches.
Height of a bar: 0.043% per inch

Suppose now you measure the lengths in feet. What's the height of the bar?

$(12 * 0.043) \% \text{ per foot}$

****Examples****

- "at random": uniformly at random
- "cards dealt from a deck": uniformly at random without replacement from standard deck (which will be described)
- coins, dice, etc fair unless otherwise specified

Questions involving multiple trials:

Ask yourself, "What does the first trial have to be?"

If you can answer that cleanly ("The first trial has to be of Type X"), almost inevitably your answer will be a product of fractions.

If there's no clear answer, ask yourself what the second trial has to be. If you can answer that cleanly, again almost inevitably your answer will be a product of fractions. If you can't answer it cleanly, then there's more work to be done:

- try partitioning the event into all the distinct ways in which it can happen
- look at the complement and hope that it's simpler than the event itself

1. Win a bet with chance $1/100$ each time, regardless of all other times. Chance of losing the first three bets: $(99/100)*(99/100)*(99/100)$

2. Bet as above. Chance of winning at least one of the first three bets: $1 - \text{answer to (1)}$

3. Bet as above. Chance of winning none of the first three bets:
same as (1)

4. Two cards dealt from a deck. Chance of heart followed by spade:

$$(13/52)*(13/51)$$

5. Two cards dealt from a deck. Chance of two different suits:

$$(52/52)*(39/51)$$

6. Four cards dealt from a deck. Chance that all four suits are different:

$$(52/52)*(39/51)*(26/50)*(13/49)$$

7. Coin lands heads with chance 0.3. Tossed twice. Chance that two different faces appear:

HT or TH

$$0.3*0.7 + 0.7*0.3$$

Also can be done this way: $1 - P(\text{HH or TT}) = 1 - (0.3*0.3 + 0.7*0.7)$

8. 5 cards, one of which has a gold star. Two cards dealt at random ****without**** replacement. Chance that second card is the one with the gold star:

1/5. Note the 5 in the denominator. The gold star card can be in any one of 5 equally likely positions

9. Standard deck of 52 cards. Deal cards (at random without replacement). Chance that the 43rd card is an ace: 4/52. Note the absence of 43 from the answer.