



Lecture 20

Causality

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Announcements

A/B Testing

- **Null:** The two samples are drawn randomly from the same underlying distribution.
 - If the null is true, all rearrangements of the variable values among the two samples are equally likely. So:
 - compute the observed test statistic
 - then shuffle the values and recompute the statistic;
repeat; compare with the observed statistic
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Deflategate

2015 AFC Championship Game



Deflategate

Wikipedia:

The 2015 AFC Championship Game football tampering scandal, commonly referred to as Deflategate, or Ballghazi

...

'Deflategate' returns, focus on Tom Brady's destroyed cellphone

POSTED 9:54 AM, MARCH 5, 2016, BY [CNN WIRE](#), UPDATED AT 10:33AM, MARCH 5, 2016

(Demo)

Null hypothesis

The 4 Colts footballs are like a sample drawn at random without replacement from all 15 balls.

- To test this hypothesis, repeat this process:
 - Randomly permute all 15 balls
 - Label 11 of them “Patriots” and the remaining 4 “Colts”
 - Compare the averages of the two groups

(Demo)

Causality

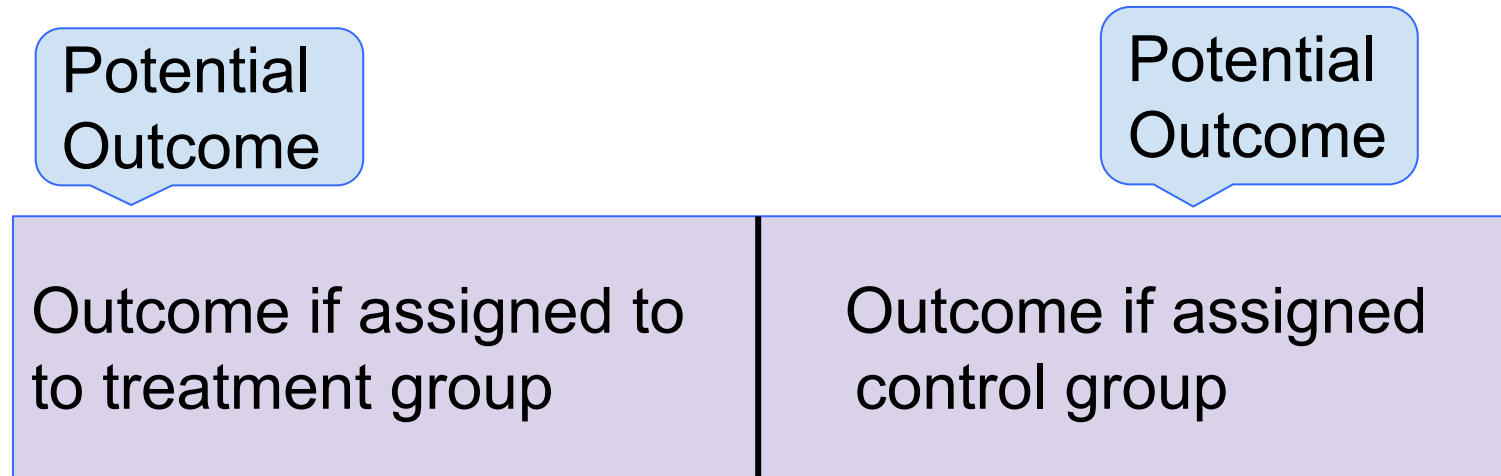
Randomized Controlled Experiment

- Sample A: **control group**
- Sample B: **treatment group**
- **If the treatment and control groups are selected at random, then you can make causal conclusions.**
- Any difference in outcomes between the two groups could be due to
 - chance
 - the treatment

(Demo)

Before the Randomization

- In the population there is one imaginary ticket for each of the 31 participants in the experiment.
- Each participant's ticket looks like this:



The Data

16 randomly picked tickets show:

	Outcome if assigned to control group
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The remaining 15 tickets show:

Outcome if assigned to treatment group	
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The Hypotheses

- **Null:**

- The distribution of all 31 potential control scores is the same as the distribution of all 31 potential treatment scores.

- **Alternative:**

- The distribution of all 31 potential control scores is different from the distribution of all 31 potential treatment scores.

(Demo)
